## UNIT 8:

## Indefinite Integration

## Specific Objectives:

1. To perform indefinite integration as the reverse process of differentiation.
2. To learn standard formulae for indefinite integration.
3. To find indefinite integrals using substitution.

|  | Detailed Content | Time Ratio | Notes on Teaching |
| :---: | :---: | :---: | :---: |
| 8.1 | Indefinite integration | 2 | The idea of primitive function is helpful and the relation $\int f(x) \mathrm{d} x=F(x)+C$ should be stressed while the meaning of $C$ be explained. |
| 8.2 | Some formulae for indefinite integration | 3 | Treating indefinite integration as the reverse process of differentiation, students should be able to find the following standard integrals: $\begin{aligned} & \int x^{n} \mathrm{~d} x, \text { when } n \neq-1 \\ & \int e^{x} \mathrm{~d} x \end{aligned}$ |
|  |  |  | It should be noted that $\int \frac{1}{x} \mathrm{~d} x=\ln \|x\|+c$ <br> Theorems on the following integrals should be taught: $\begin{aligned} & \int k f(x) \mathrm{d} x=k \int f(x) \mathrm{d} x \\ & \int[f(x) \pm g(x)] \mathrm{d} x=\int f(x) \mathrm{d} x \pm \int g(x) \mathrm{d} x \end{aligned}$ |
| 8.3 | Integration by substitution | 4 | The following integrals may be used as examples in introducing the topic: $\int(2 x+1)^{5} \mathrm{~d} x \text { and } \int 2 x \sqrt{x^{2}+1} \mathrm{~d} x$ <br> Different methods of evaluating the same integral may lead to different results, but these can only differ by a constant. <br> e.g. $\int(x+1) \mathrm{d} x=\frac{(x+1)^{2}}{2}+C_{1}$ $\int(x+1) \mathrm{d} x=\frac{x^{2}}{2}+x+C_{2}$ <br> It should be noted that integration by parts is not required. |

