

Exemplar 12 : Verifying Points Lying on the Line Do Satisfy the Linear Equation

Objective : To verify that points lying on the line will satisfy the linear equation

Key Stage : 3

Learning Unit : Linear Equations in Two Unknowns

Material Required : Dynamic geometry software such as *Geometer's Sketchpad*

Prerequisite Knowledge :

- (1) Coordinates
- (2) Simple substitution
- (3) Graphical representation of a linear equation.

Description of the Activity :

1. Before the lesson, the teacher uses a dynamic geometry software such as *Geometer's Sketchpad* to prepare the graph $y = x + 1$. The graph is shown in Figure 1 and is used as an illustration for the activity.

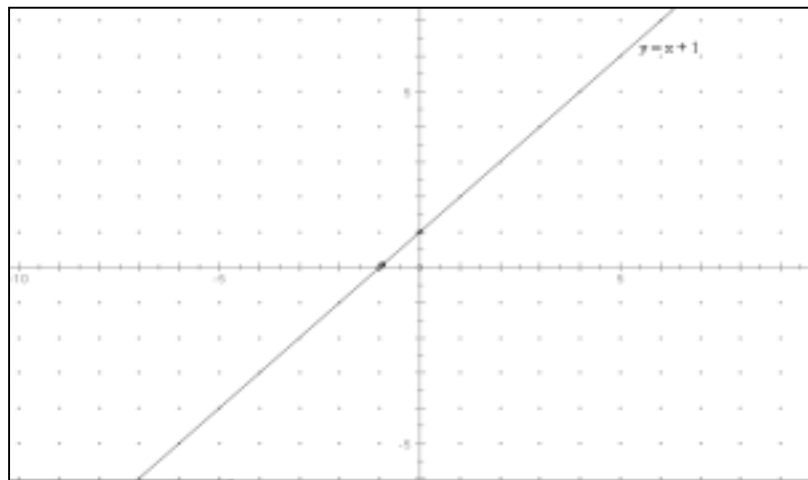


Figure 1

- An arbitrary point on the straight line in Figure 2 is plotted and labelled as “A”. Students calculate the values of the two data “y-coordinate” and “x-coordinate plus 1” for the point A. See Figure 2.

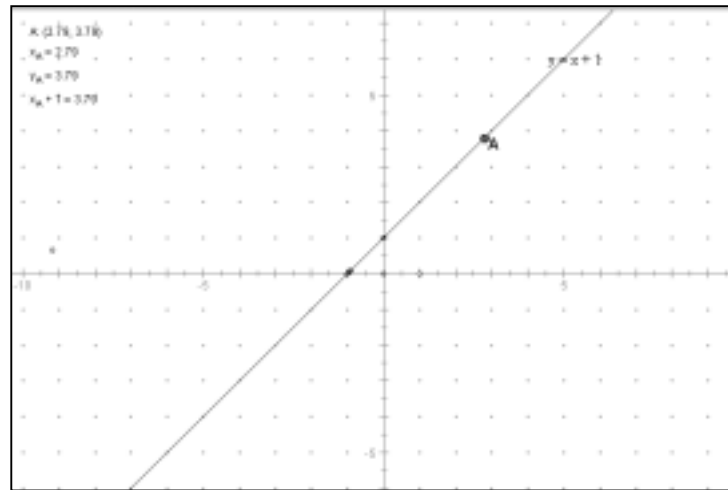


Figure 2

- The teacher asks students to drag the point A along the straight line and observe the change in values of y_A and $x_A + 1$. They are expected to find that these two values are equal no matter where the point is.
- The teacher instructs students to add a point B in the graph, which does not lie on the straight line. Students measure its coordinates (x_B, y_B) and calculate the values of y_B and $x_B + 1$. See Figure 3.

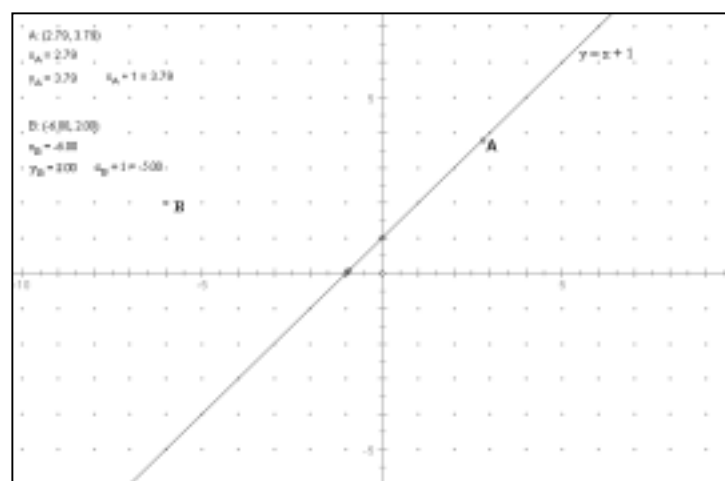


Figure 3

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5. The teacher asks students to move the point B freely on the coordinate plane and observe the values of y_B and $x_B + 1$. They are expected to find that these two values are not equal unless B lies on the straight line.
 6. For more able students, the teacher can ask them what pattern they can find from observing the changes in the values of y_B and $x_B + 1$. If necessary, the teacher may guide students by asking the following questions:
 - (a) Which one is greater? Where does this happen?
 - (b) How can you explain these findings?
 7. The teacher guides students to draw the following conclusion:

If the point (x, y) lies on a straight line, the corresponding values of x and y satisfy the equation of the given line.

If the point (x, y) does not lie on the straight line, the corresponding values of x and y do not satisfy the equation of the given line.
 8. The teacher can further ask students the following questions:
 - (a) How many points lie on the graph?
 - (b) How many ordered pairs satisfy the equation of the line?
 9. The teacher introduces the “Algebraic Method” for students to determine whether a point lies on a given straight line:
 - (a) Substitute the values of the x -coordinate and y -coordinate into the Left Hand Side and the Right Hand Side of the equation of the line.
 - (b) Compare these two values.
 - (c) If they are equal, the given point lies on the line. Otherwise, the point does not lie on the line.
 10. Students repeat the steps in Points 2 to 6 and Point 9 for the following graphs to consolidate the concepts in Point 7.
 - (a) $y = -0.5x - 1$
 - (b) $y = 2x + 3$.

Notes for Teachers :

1. The teacher should discuss with students that there are infinitely many points that lie on the graph of a linear equation, and hence there are infinitely many ordered pairs that satisfy a linear equation.

2. (a) For more able students, they are expected to find out that if point B lies on the upper half-plane then $y > x + 1$ while if point B lies on the lower half-plane then $y < x + 1$. The teacher should point out that this conclusion (the “direction” of the inequality sign) does not hold for some linear equations in standard form. For example, consider the graph of $x - y + 1 = 0$. Points that satisfy the inequality $x - y + 1 < 0$ lie on the upper half-plane while points that satisfy the inequality $x - y + 1 > 0$ lie on the lower half-plane.
(b) When point B lies on the straight line, then the equation of the straight line is $y = x + 1$. Furthermore, the teacher can explain that any straight line divides the plane into three distinct parts, namely the upper half-plane, the line and the lower half-plane.

3. The teacher may also consider horizontal and vertical lines in the activity.