Thinking Skills

Exemplar 6



Exemplar 6 : A Game of Dice

Objectives: Students will be able to

- 1. investigate probabilities in real-life activities;
- 2. consolidate the relation between empirical and theoretical probabilities.

Dimension : Data Handling

Learning Unit: Simple Idea of Probability

Key Stage: 3

Materials Required: Dice, transparencies and overhead projector

Prerequisite Knowledge: Meaning of probability, calculations of empirical and

theoretical probabilities

Main HOTS Involved: Inquiring Skills

Description of the Activity:

- 1. Divide students in pairs. One of them is called "Mr. L" and the other is "Mr. H".
- 2. Assign a group number to each pair and give them two dice.
- 3. Ask students to perform the following game:
 - (a) Throw two dice 25 times.
 - (b) In each throw, subtract the smaller number from the larger. The answer is called "Dice Difference".
 - (c) If the "Dice Difference" is 0, 1 or 2, then Mr. L wins. If the "Dice Difference" is 3, 4 or 5, Mr. H wins.
- 4. Instruct each group to enter their results in Worksheet 6.1 provided.

5. Ask students to complete Table 6.1 printed on a transparency:

Group number	Number of times Mr. L wins	Number of times Mr. H wins
1		
2		
3		
4		
5		
6		
7		
8		
9		
10		
11		
12		
13		
14		
15		
16		
17		
18		
19		
20		
Total		

Table 6.1

- 6. Discuss the following questions with students:
 - (a) What is the empirical probability that Mr. L wins in each group? (The teacher can add one more column to Table 6.1 and write down the answers.)
 - (b) Is there any pattern found in (a)?
 - (c) Does the game seem to be fair to both players? Why? At this moment, the teacher does not make any comments on students' findings.

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- 7. Ask students to use the data obtained in Table 6.1 to complete Worksheet 6.2.
- 8. Discuss the following questions with students:
 - (a) What will the empirical probability that Mr. L wins tend to in the long run?
 - (b) What will the empirical probability that Mr. H wins tend to in the long run?
 - (c) Is the game fair to both players? What conclusion can be drawn?
- 9. By using the grid paper or any other method, list out the sample space of the outcomes of throwing two dice and then determine the numbers of favorable outcomes (i.e. Mr. L or Mr. H wins).
- 10. Students are guided to draw conclusions from the theoretical probability that each player wins and determine whether the game is fair or not.
- 11. If the game is not fair, ask students to modify the rules and make it fair.
- 12. Give justifications for their suggestions.

Worksheet 6.1

Please tick the appropriate box.

No. of Throw	Mr. L wins	Mr. H wins
1		
2		
3		
4		
5		
6		
7		
8		
9		
10		
11		
12		
13		
14		
15		
16		
17		
18		
19		
20		
21		
22		
23		
24		
25		
Total no. of wins		

Who is the winner? ____

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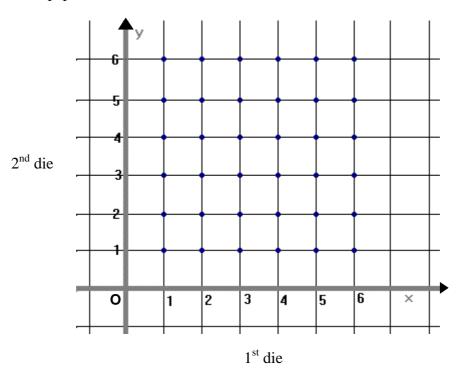
Worksheet 6.2

Please complete the following table.

Group number	Accumulated number	Number of	Empirical probability
less than or equal to	of times Mr. L wins	rounds played	that Mr. L wins
1		25	
2		50	
3		75	
4		100	
5		125	
6		150	
7		175	
8		200	
9		225	
10		250	
11		275	
12		300	
13		325	
14		350	
15		375	
16		400	
17		425	
18		450	
19		475	
20		500	

Notes for Teachers:

- 1. Throughout the game, students will experience that the empirical probability will get close to the theoretical probability as the number of trials increases.
- 2. Students can use (a) a grid paper; (b) ordered pairs; (c) the tabulation method to show all possible outcomes when two dice are thrown.
 - (a) Grid paper



(b) Ordered pairs

	<u>.</u>	1 st die					
		1	2	3	4	5	6
2 nd die	1	(1,1)	(2,1)	(3,1)	(4,1)	(5,1)	(6,1)
	2	(1,2)	(2,2)	(3,2)	(4,2)	(5,2)	(6,2)
	3	(1,3)	(2,3)	(3,3)	(4,3)	(5,3)	(6,3)
	4	(1,4)	(2,4)	(3,4)	(4,4)	(5,4)	(6,4)
	5	(1,5)	(2,5)	(3,5)	(4,5)	(5,5)	(6,5)
	6	(1,6)	(2,6)	(3,6)	(4,6)	(5,6)	(6,6)

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(c) Tabulation method

Dice Difference	Favorable outcomes in ordered pairs				
0	(1,1) (2,2) (3,3) (4,4) (5,5) (6,6)				
1	(1,2) (2,3) (3,4) (4,5) (5,6) (2,1) (3,2) (4,3) (5,4) (6,5)				
2	(1,3) (2,4) (3,5) (4,6) (3,1) (4,2) (5,3) (6,4)				
3	(1,4) (2,5) (3,6) (4,1) (5,2) (6,3)				
4	(1,5) (2,6) (5,1) (6,2)				
5	(1,6) (6,1)				

3. Study the following table.

Dice Difference	0	1	2	3	4	5
Total number of favorable outcomes	6	10	8	6	4	2

This game is not fair since the theoretical probability of Mr. L wins is $\frac{6+10+8}{36} = \frac{2}{3}$ and that of Mr. H is $\frac{6+4+2}{36} = \frac{1}{3}$.

4. Suggestion for modifying the rules to make the game more fair:

Replace Mr. L and Mr. H by Mr. E and Mr. O. Mr. E wins if the dice difference is 0, 2 or 4 and Mr. O wins if the dice difference is 1, 3 or 5.

Justification:

P(Mr. E wins) =
$$\frac{6+8+4}{36} = \frac{1}{2}$$
 P(Mr. O wins) = $\frac{10+6+2}{36} = \frac{1}{2}$

Accept other modifications from students provided that the two players have equal chance of winning.